

# IB Maths: AA HL

## Kinematics

### Topic Questions

These practice questions can be used by students and teachers and is Suitable for IB Maths AA HL Topic Questions

Course	IB Maths
Section	5. Calculus
Topic	5.6 Kinematics
Difficulty	Medium

**Level: IB Maths**

**Subject: IB Maths AA HL**

**Board: IB Maths**

**Topic: Kinematics**

## Question 1

A skydiver jumps from a moving aircraft at a point directly above a fixed point,  $O$ , on the ground. The trajectory of the skydiver is then modelled by the function

$$h(x) = 3200 - 0.5x^2$$

where  $h$  m is the height of the skydiver above the ground and  $x$  m is the horizontal distance along the ground from point  $O$ .

- (a) (i) Explain the significance of the value 3200 in the model.
- (ii) Calculate the horizontal distance the skydiver covered upon landing.

[2 marks]

(b) Sketch a graph of  $h$  against  $x$ .

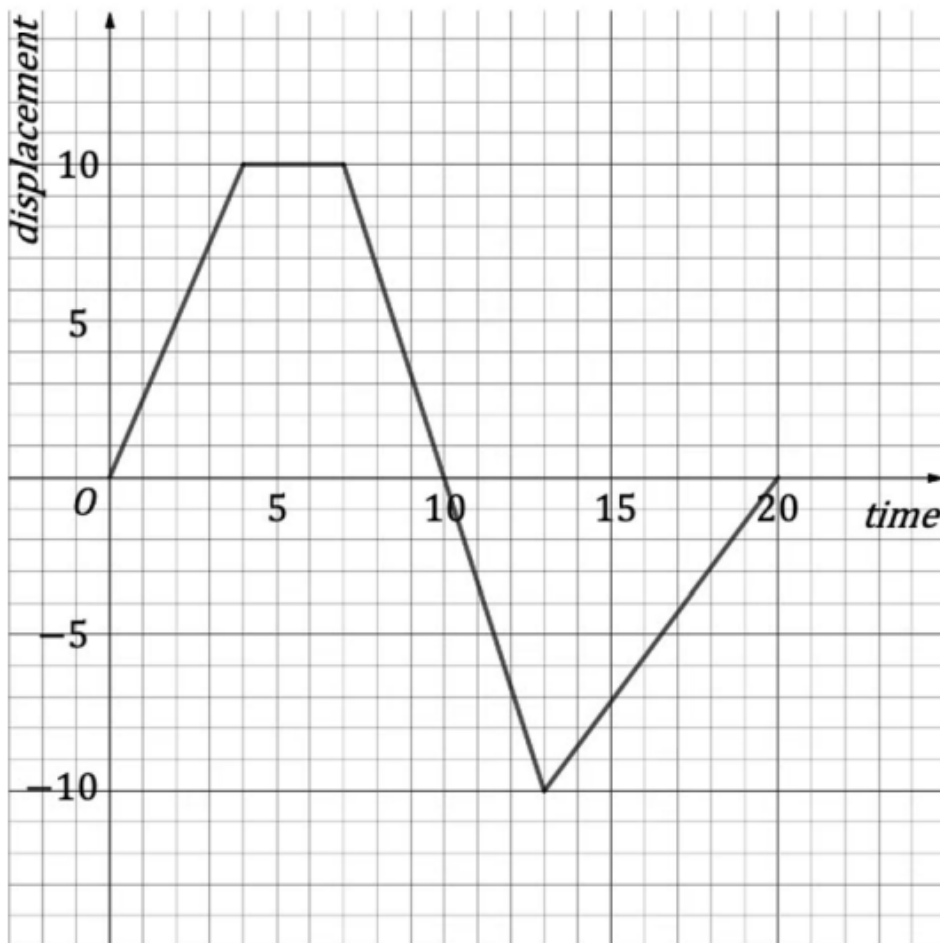
[2 marks]

(c) Explain why the model is not suitable for values of  $x$  larger than 80 m.

[1 mark]

## Question 2

A particle moves along a horizontal line starting at the point  $O$ . The displacement-time graph for the first 20 seconds of its motion is shown below. Displacement is measured in metres.



- (a) (i) Write down the displacement of the particle after 2 seconds.  
(ii) Write down the displacement of the particle after 4 seconds.

[2 marks]

(b) Find the velocity of the particle between 13 and 20 seconds.

[1 mark]

(c) Find the speed of the particle between 7 and 10 seconds.

[1 mark]

(d) Find the total distance travelled by the particle after 20 seconds.

[2 marks]

### Question 3

A cricket ball is projected directly upwards from ground level. The motion of the cricket ball is modelled by the function

$$h(t) = 13t - 4.9t^2 \quad t > 0$$

where  $h$  metres is the height of the cricket ball above ground level after  $t$  seconds.

(a) Find the times at which the cricket ball is exactly 3 m above the ground.

[2 marks]

(b) For how long is the cricket ball at least 3 m above the ground?

[1 mark]

A player catches the cricket ball (on its way down) at a height of 0.8 m above the ground.

(c) Find the length of time the ball was in the air.

[2 marks]

(d) Find the total distance travelled by the ball.

[2 marks]

(e) Find the velocity of the cricket ball at  $t = 1$  second.

[2 marks]

#### Question 4

A soft ball is thrown upwards from the top of a 10 m tall building.

The height,  $h$  m of the ball above the ground after  $t$  seconds is modelled by the function

$$h(t) = H + 7.8t - 4.9t^2 \quad t > 0$$

(a) Write down the value of  $H$ .

[1 mark]

(b) Find the height of the ball after 2 seconds.

[2 marks]

(c) Find the time at which the ball is at the same height as it was when thrown.

[2 marks]

(d) Find the time the ball first hits the ground.

[2 marks]

(e) Find  $h''(t)$  and hence show that the acceleration at any time is  $-9.8 \text{ m/s}^2$ .

[3 marks]

### Question 5

A particle moves along a straight line with a velocity,  $v \text{ ms}^{-1}$ , given by  $v = 2^t - 2$  where  $t$  is measured in seconds such that  $0 \leq t \leq 4$ .

(a) Find the acceleration of the particle at time  $t = 2$ .

[2 marks]

(b) State the time when the particle comes to rest.

[1 mark]

(c) Find the total distance travelled by the particle.

[3 marks]

### Question 6

A particle is found to have an acceleration,  $a \text{ ms}^{-2}$ , according to the function

$$a = \frac{1}{t^2} + \sin t, \text{ where } t \geq 1$$

(a) Find an expression for the velocity,  $v$ , of the particle given that  $v(1) = 1$ .

[4 marks]

(b) Find the velocity of the particle at  $t = 2$ .

[2 marks]

### Question 6

A particle, moving in a straight line, is found to have a velocity  $v = \sin t + \cos 2t$  where  $v$  is measured in  $\text{ms}^{-1}$  and time  $t$  is measured in seconds such that  $0 \leq t \leq 5$ .

(a) Find the time(s) when the particle is instantaneously at rest.

[2 marks]

(b) Find the time(s) when the particle changes direction.

[1 mark]

(c) Find the distance travelled in the first second of motion.

[3 marks]

(d) Find the acceleration of the particle at the instant it first changes direction.

[3 marks]

(e) Find the displacement of the particle from its starting point to the point when  $t = 5$ .

[4 marks]