

Mathematics: analysis and approaches Standard level Paper 1

14 May 2026

Zone A afternoon | Zone B afternoon | Zone C afternoon

Session number

1 hour 30 minutes

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Instructions to students

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- You are not permitted access to any calculator for this paper.
- Section A: answer all questions. Answers must be written within the answer boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number on the front of the answer booklet, and attach it to this examination paper and your cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **mathematics: analysis and approaches SL formula booklet** is required for this paper.
- The maximum mark for this examination paper is **[80 marks]**.

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10 pages

2226–5018

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Full marks are not necessarily awarded for a correct answer with no working. Answers must be supported by working and/or explanations. Where an answer is incorrect, some marks may be given for a correct method, provided this is shown by written working. You are therefore advised to show all working.

Section A

Answer **all** questions. Answers must be written within the answer boxes provided. Working may be continued below the lines, if necessary.

1. [Maximum mark: 6]

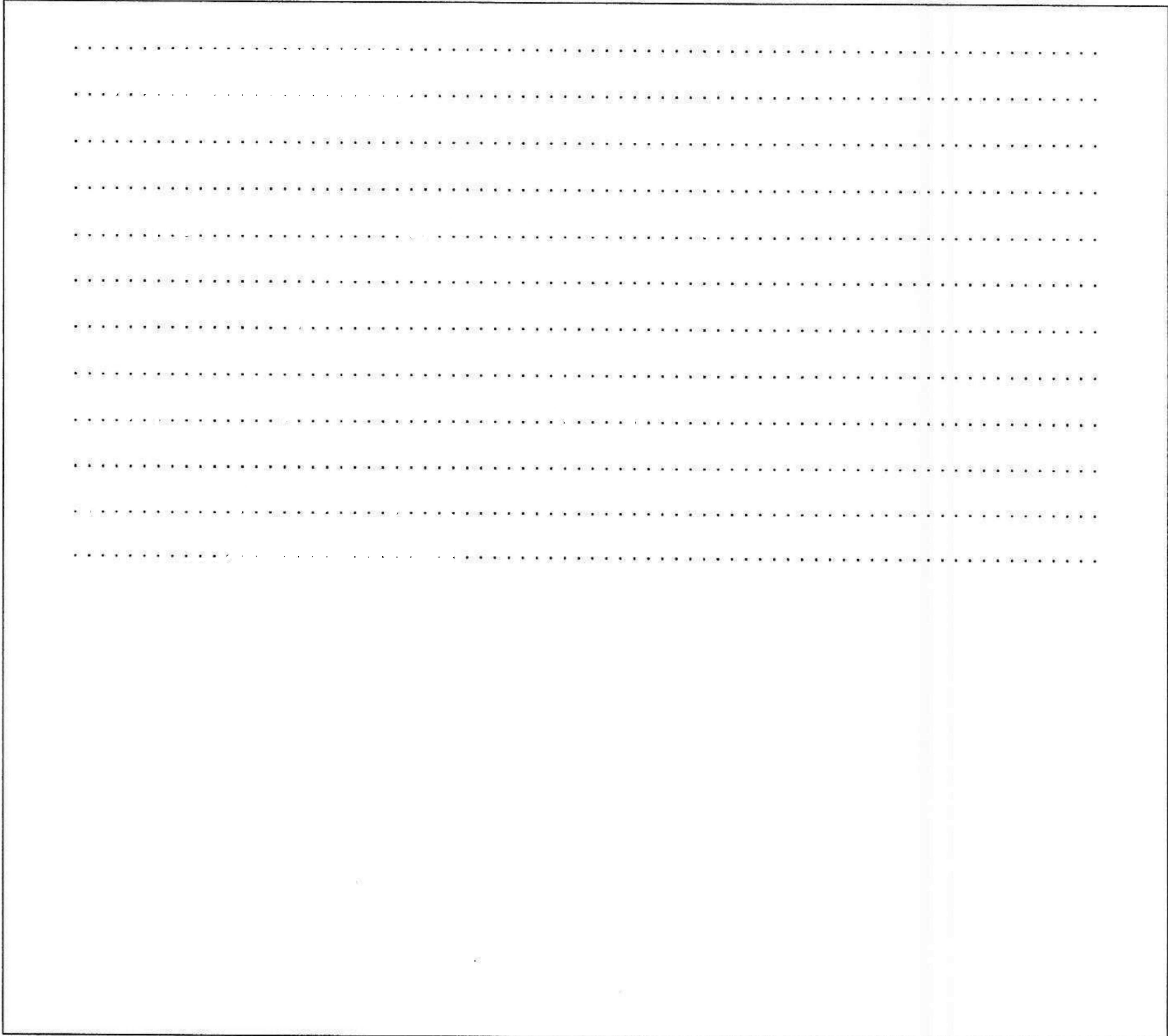
Consider the function $f(x) = 2x + \sin x, x \in \mathbb{R}$.

(a) Find $f'(x)$. [2]

(b) Hence, find the equation of the tangent to the graph of f at the point where $x = \pi$. [4]

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5. [Maximum mark: 7]

(a) Show that $\log_{25}(81x^2) = \log_5 9 + \log_5 x$ for $x > 0$. [4]

(b) Hence, solve the equation $\log_5 \sqrt[3]{x} = \log_{25}(81x^2) - \log_5 4$, where $x > 0$. [3]

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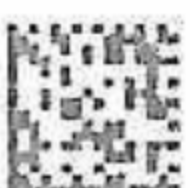
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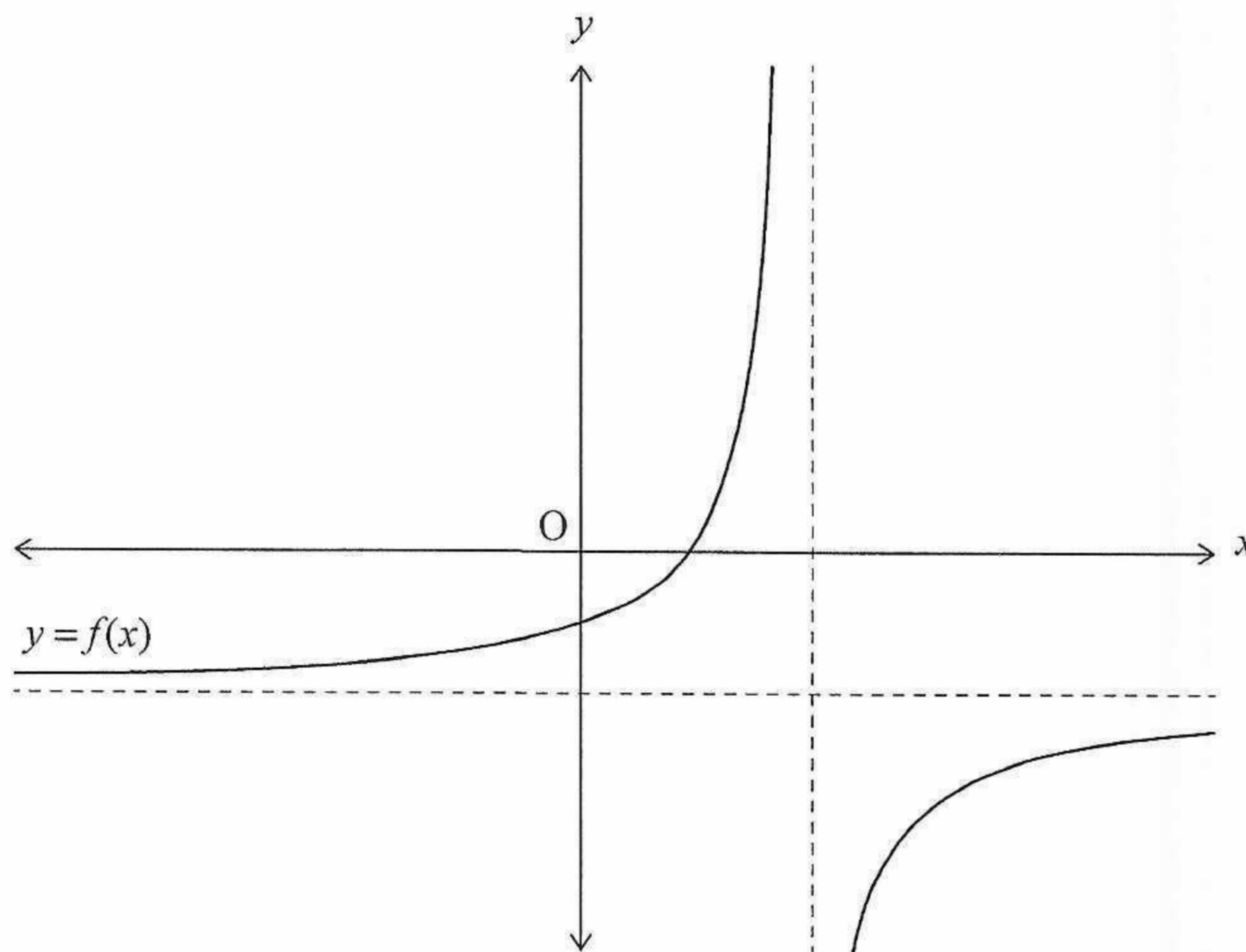
Section B

Answer all questions in the answer booklet provided. Please start each question on a new page.

7. [Maximum mark: 12]

Consider the function $f(x) = \frac{2x-3}{3-x}$, $x \in \mathbb{R}$, $x \neq 3$.

The graph of f and its asymptotes are shown in the following diagram.



- (a) Find the equation of
 - (i) the vertical asymptote;
 - (ii) the horizontal asymptote. [3]
- (b) Find the coordinates of the points where the graph of f intersects the coordinate axes. [4]

Consider the function $g(x) = x + 4$, $x \in \mathbb{R}$.

- (c) (i) Describe the transformation that transforms the graph of $y = f(x)$ to the graph of $y = (g \circ f)(x)$.
- (ii) Hence, find the range of $g \circ f$. [5]



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8. [Maximum mark: 15]

Consider the function $f(x) = ax^3 + bx^2 + cx + d$, where $x \in \mathbb{R}$ and where a, b, c and d are real constants.

The graph of f has a point of inflexion at $(-2, -2c + d + 24)$.

(a) Show that $a = \frac{3}{2}$ and $b = 9$. [6]

It is given that the tangents to the graph of f at $x = -3$ and $x = k$ are horizontal.

- (b) (i) Show that $c = \frac{27}{2}$.
- (ii) Find the value of k .
- (iii) State whether f has a local maximum or a local minimum at $x = k$, justifying your answer. [7]

The graph of f intersects the y -axis at the point P .

(c) Show that the tangent to the graph of f at $x = -3$ passes through P . [2]

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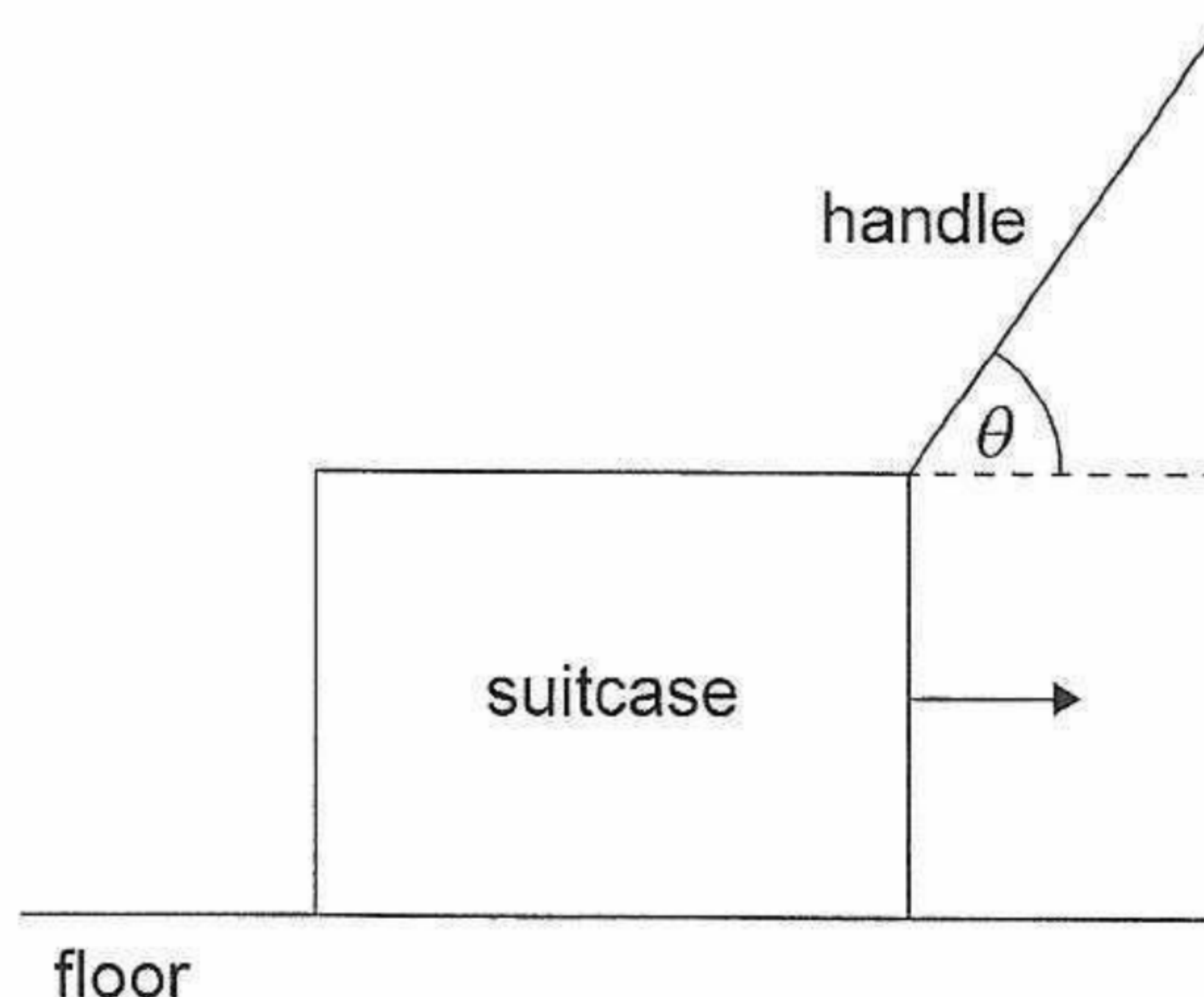
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9. [Maximum mark: 15]

Eleanor uses the handle on a heavy suitcase to pull it so that it moves horizontally along the floor.

The handle makes an angle of θ radians with the horizontal, as shown in the following diagram.

diagram not to scale



The magnitude, F Newtons, of the minimum force that Eleanor needs to apply to make the suitcase move horizontally when the handle makes an angle of θ radians is given by

$$F(\theta) = \frac{A}{\cos \theta + \mu \sin \theta}, \text{ where } 0 \leq \theta < \frac{\pi}{2} \text{ and } \mu \in \mathbb{R}.$$

When the handle is horizontal, $F = 300$.

(a) Show that $A = 300$. [2]

In the case when $\theta = \frac{\pi}{6}$, $F = 100\sqrt{3}$.

(b) Show that $\mu = \sqrt{3}$. [4]

Eleanor wishes to minimize the magnitude of the force she needs to apply to make the suitcase move horizontally. In order to achieve this, she needs to hold the handle at the angle α , where $0 < \alpha < \frac{\pi}{2}$.

(c) (i) Show that $\frac{dF}{d\theta} = \frac{300(\sin \theta - \sqrt{3} \cos \theta)}{(\cos \theta + \sqrt{3} \sin \theta)^2}$.
 (ii) Hence, show that $\alpha = \frac{\pi}{3}$ and find the corresponding value of $F(\alpha)$. [9]

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