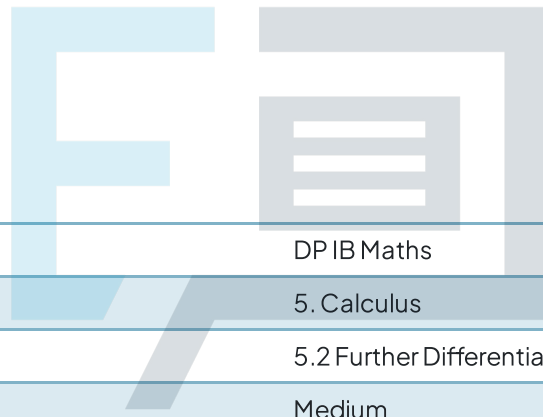




5.2 Further Differentiation

Question Paper



| | |
|------------|-----------------------------|
| Course | DP IB Maths |
| Section | 5. Calculus |
| Topic | 5.2 Further Differentiation |
| Difficulty | Medium |

Exam Papers Practice

To be used by all students preparing for DP IB Maths AA SL
Students of other boards may also find this useful

Question 1

Differentiate $\frac{5x^7}{\sin 2x}$ with respect to x .

[4 marks]

Question 2a

Find $\frac{dy}{dx}$ for each of the following:

$$y = \cos(x^2 - 3x + 7) + \sin(e^x)$$



[4 marks]

Exam Papers Practice

Question 2b

$$y = \ln(2x^3)$$

[3 marks]

Question 3a

Differentiate with respect to x , simplifying your answers as far as possible:

$$(4 \cos x - 3 \sin x)e^{3x-5}$$

[3 marks]



Question 3b

$$(x^3 - 4x^2 + 7) \ln x$$

[3 marks]

Exam Papers Practice

Question 4

A curve has the equation $y = e^{-3x} + \ln x$, $x > 0$.

Find the gradient of the normal to the curve at the point $(1, e^{-3})$, giving your answer correct to 3 decimal places.

[4 marks]

Question 5

Find the equation of the tangent to the curve $y = e^{3x^2+5x-2}$ at the point $(-2, 1)$, giving your answer in the form $ax + by + c = 0$, where a , b and c are integers.

[4 marks]



Exam Papers Practice

Question 6

Let $f(x) = \frac{g(x)}{h(x)}$, where $g(2) = 4$, $h(2) = -1$, $g'(2) = 0$ and $h'(2) = 2$

Find the equation of the tangent of f at $x = 2$.

[6 marks]

Question 7a

A curve has the equation $y = x^3 - 12x + 7$.

Find expressions for $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$.

[3 marks]

Question 7b

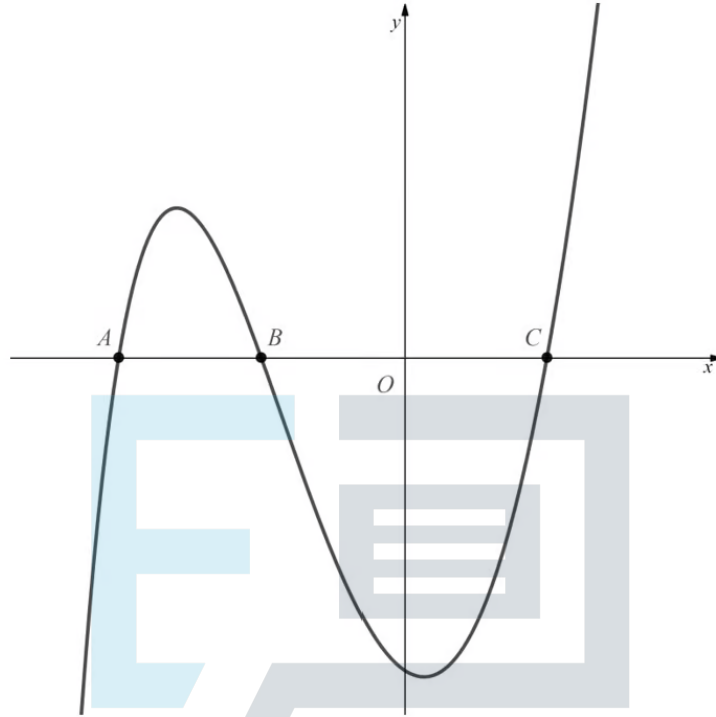
Determine the coordinates of the local minimum of the curve.

[3 marks]

Question 8a

The diagram below shows part of the graph of $y = f(x)$, where $f(x)$ is the function defined by

$$f(x) = (x^2 - 1) \ln(x + 3), \quad x > -3$$



Points A , B and C are the three places where the graph intercepts the x -axis.

Find $f'(x)$.

Exam Papers Practice [4 marks]

Question 8b

Show that the coordinates of point A are $(-2, 0)$.

[2 marks]

Question 8c

Find the equation of the tangent to the curve at point A .

[3 marks]

Question 9a

Let $f(x) = x^2e^x$.

Find $f'(x)$.



[3 marks]

Exam Papers Practice

Question 9b

Find $f''(x)$.

[3 marks]

Question 9c

Find the exact x of the points of inflection for the graph of f .

[4 marks]



Question 9d

Find $\lim_{x \rightarrow -2} x^2 e^x$.

[1 mark]

Exam Papers Practice

Question 10a

Let $f(x) = 2e^{2\cos x}$, where $-\pi \leq x \leq \pi$.

Find the number of points containing a horizontal tangent.

[1 mark]

Question 10b

Show algebraically that the gradient of the tangent at $x = \frac{\pi}{2}$ is -4 .

[4 marks]

Question 10c

State the gradient of the tangent at $x = \frac{3\pi}{2}$.

[1 mark]

Question 10d

It can be found that as the function, f , undergoes a transformation $f(kx)$, the number of stationary points found between $-\pi \leq x \leq \pi$ increases.

Find the number of stationary points on f after a transformation of $f(2x)$ and hence, state the general rule representing the number of stationary points in terms of k where $k \in \mathbb{Z}^+$.

[3 marks]

Exam Papers Practice

Question 11

Let $f(x) = \sin x$ and $g(x) = \sin^2 x$, for $0 \leq x \leq 2\pi$.

Solve $f'(x) = g'(x)$.

[5 marks]