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# 4.1 Scalars & Vectors

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## PHYSICS

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# AQA A Level Revision Notes

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## 4.1 Scalars & Vectors

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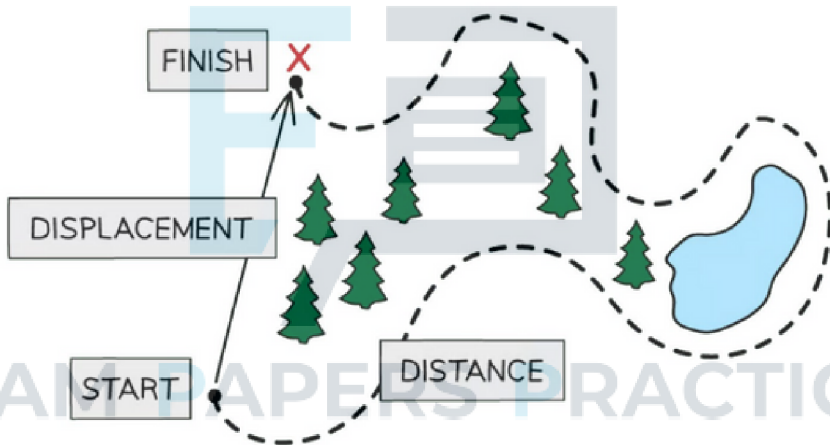


# EXAM PAPERS PRACTICE

## 4.1.1 Scalars &amp; Vectors

### Scalars & Vectors

- A **scalar** is a quantity which **only** has a magnitude (size)
- A **vector** is a quantity which has **both** a magnitude and a direction
- For example, if a person goes on a hike in the woods to a location which is a couple of miles from their starting point
  - As the crow flies, their **displacement** will only be a few miles but the **distance** they walked will be much longer



***Displacement is a vector while distance is a scalar quantity***

- **Distance** is a scalar quantity because it describes how far an object has travelled overall, but not the direction it has travelled in
- **Displacement** is a vector quantity because it describes how far an object is from where it started and in what direction
- Some common scalar and vector quantities are shown in the table below:



## Scalars and Vectors Table

SCALARS	VECTORS
DISTANCE	DISPLACEMENT
SPEED	VELOCITY
MASS	ACCELERATION
TIME	FORCE
ENERGY	MOMENTUM
VOLUME	
DENSITY	
PRESSURE	
ELECTRIC CHARGE	
TEMPERATURE	

**Exam Tip**

Do you have trouble figuring out if a quantity is a vector or a scalar? Just think - can this quantity have a minus sign? For example - can you have negative energy? No. Can you have negative displacement? Yes!



## Combining Vectors

- **Vectors** are represented by an arrow
  - The arrowhead indicates the **direction** of the vector
  - The length of the arrow represents the **magnitude**
- Vectors can be combined by **adding** them to produce the resultant vector
  - The resultant vector is sometimes known as the 'net' vector (eg. the net force)
- There are two methods that can be used to add vectors
  - **Calculation** – if the vectors are perpendicular
  - **Scale drawing** – if the vectors are not perpendicular

### Vector Calculation

- Vector calculations will be limited to two vectors at right angles
- This means the combined vectors produce a right-angled triangle and the magnitude (length) of the resultant vector is found using **Pythagoras' theorem**

MAGNITUDE OF THE RESULTANT VECTOR, R

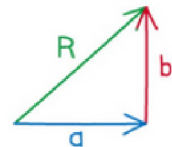
1 ADD TWO VECTORS  $a$  &  $b$



2 LINK THE VECTORS HEAD-TO-TAIL

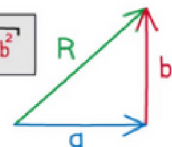


3 FORM THE RESULTANT VECTOR FROM LINKING THE TAIL OF  $a$  TO THE HEAD OF  $b$



4 CALCULATE R USING PYTHAGORAS' THEOREM

$$R = \sqrt{a^2 + b^2}$$



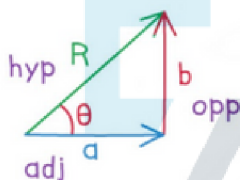
*The magnitude of the resultant vector is found by using Pythagoras' Theorem*



- The direction of the resultant vector is found from the angle it makes with the horizontal or vertical
  - The question should imply which angle it is referring to (ie. Calculate the angle from the x-axis)
- Calculating the angle of this resultant vector from the horizontal or vertical can be done using **trigonometry**
  - Either the sine, cosine or tangent formula can be used depending on which vector magnitudes are calculated

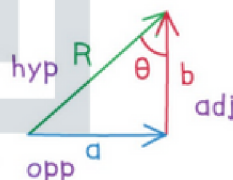
### DIRECTION OF THE RESULTANT VECTOR, R

ANGLE OF R FROM THE HORIZONTAL



$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{b}{a}$$

ANGLE OF R FROM THE VERTICAL

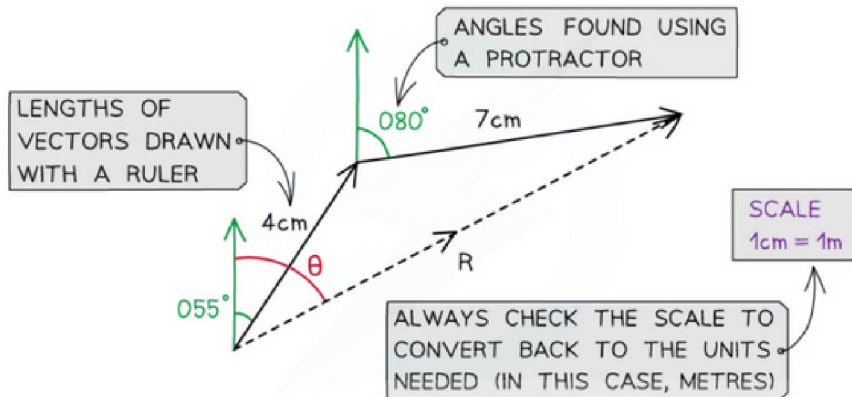


$$\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{a}{b}$$

*The direction of vectors is found by using trigonometry*

### Scale Drawing

- When two vectors are not at right angles, the resultant vector can be calculated using a scale drawing
  - **Step 1:** Link the vectors head-to-tail if they aren't already
  - **Step 2:** Draw the resultant vector using the triangle or parallelogram method
  - **Step 3:** Measure the length of the resultant vector using a ruler
  - **Step 4:** Measure the angle of the resultant vector (from North if it is a bearing) using a protractor



**A scale drawing of two vector additions. The magnitude of resultant vector  $R$  is found using a ruler and its direction is found using a protractor**

- Note that with scale drawings, a scale may be given for the diagram such as  $1\text{ cm} = 1\text{ km}$  since only limited lengths can be measured using a ruler
- The final answer is always converted back to the units needed in the diagram
  - Eg. For a scale of  $1\text{ cm} = 2\text{ km}$ , a resultant vector with a length of  $5\text{ cm}$  measured on your ruler is actually  $10\text{ km}$  in the scenario
- There are two methods that can be used to combine vectors: the **triangle method** and the **parallelogram method**
- To combine vectors using the triangle method:
  - **Step 1:** link the vectors head-to-tail
  - **Step 2:** the resultant vector is formed by connecting the tail of the first vector to the head of the second vector
- To combine vectors using the parallelogram method:
  - **Step 1:** link the vectors tail-to-tail
  - **Step 2:** complete the resulting parallelogram
  - **Step 3:** the resultant vector is the diagonal of the parallelogram

## Vector Addition



Draw the vector  $c = a + b$



TRIANGLE METHOD

STEP 1: LINK THE VECTORS  
HEAD-TO-TAIL

STEP 2: FORM THE RESULTANT  
VECTOR FROM LINKING THE TAIL  
OF  $a$  TO THE HEAD OF  $b$



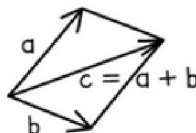
PARALLELOGRAM METHOD

STEP 1: LINK THE VECTORS  
TAIL-TO-TAIL

STEP 2: COMPLETE THE  
RESULTING PARALLELOGRAM



STEP 3: THE RESULTANT VECTOR  
IS THE DIAGONAL OF THE PARALLELOGRAM



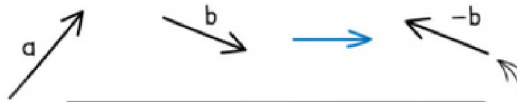




## Vector Subtraction



Draw the vector  $c = a - b$

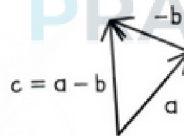


FIRST REVERSE THE DIRECTION OF VECTOR  $b$  TO MAKE  $-b$

TRIANGLE METHOD

STEP 1: LINK THE VECTORS HEAD-TO-TAIL

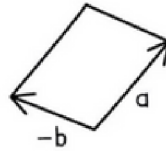
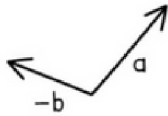
STEP 2: FORM THE RESULTANT VECTOR BY LINKING THE TAIL OF  $a$  TO THE HEAD OF  $-b$



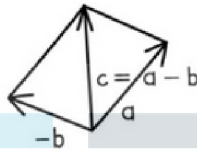
PARALLELOGRAM METHOD

STEP 1: LINK THE VECTORS TAIL-TO-TAIL

STEP 2: COMPLETE THE RESULTING PARALLELOGRAM



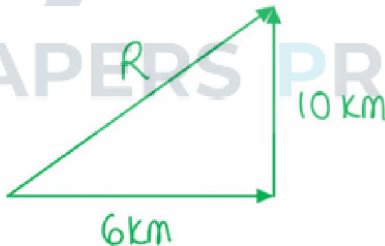
STEP 3: THE RESULTANT VECTOR IS THE DIAGONAL OF THE PARALLELOGRAM



### Worked Example

A hiker walks a distance of 6 km due east and 10 km due north. Calculate the magnitude of their displacement and its direction from the horizontal

Step 1: Draw a vector diagram

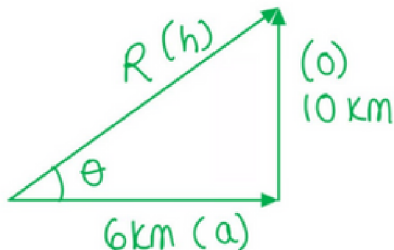


Step 2: Calculate the magnitude of the resultant vector using Pythagoras' Theorem

$$R = \sqrt{6^2 + 10^2}$$



Step 3: Calculate the direction of the resultant vector using trigonometry



$$\tan(\theta) = \frac{\text{opposite}}{\text{adjacent}} = \frac{10}{6}$$

$$\theta = \tan^{-1}\left(\frac{10}{6}\right) = 59^\circ$$



#### Exam Tip

Pythagoras' Theorem and trigonometry are consistently used in vector addition, so make sure you're fully confident with the maths here!

### 4.1.2 Resolving Vectors

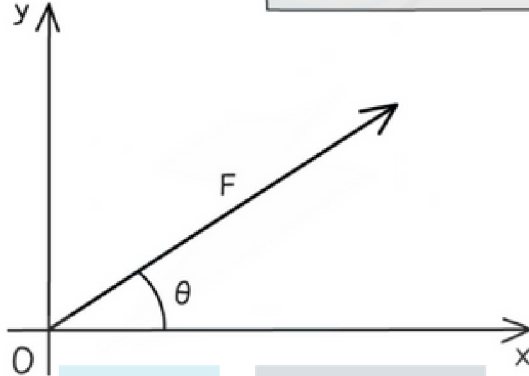
## EXAM PAPERS PRACTICE

### Resolving Vectors

- Two vectors can be represented by a single **resultant vector**
  - Resolving a vector is the opposite of adding vectors
- A single resultant vector can be resolved
  - This means it can be represented by **two** vectors, which in combination have the same effect as the original one
- When a single resultant vector is broken down into its **parts**, those parts are called **components**
- For example, a force vector of magnitude  $F$  and an angle of  $\theta$  to the horizontal is shown below

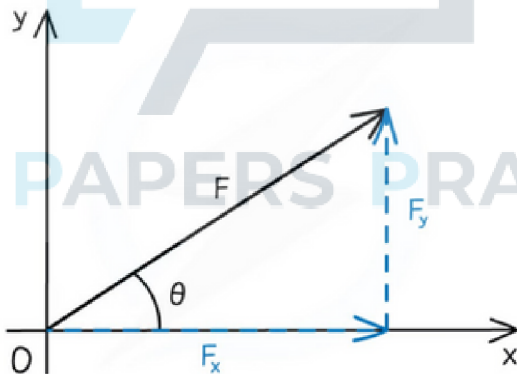


F IS A RESULTANT VECTOR



*The resultant force  $F$  at an angle  $\theta$  to the horizontal*

- It is possible to **resolve** this vector into its **horizontal** and **vertical** components using trigonometry



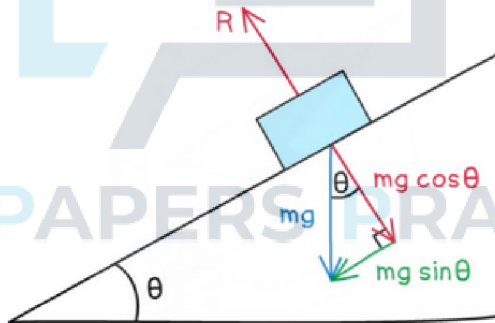


*The resultant force  $F$  can be split into its horizontal and vertical components*

- For the **horizontal** component,  $F_x = F \cos \theta$
- For the **vertical** component,  $F_y = F \sin \theta$

### Forces on an Inclined Plane

- Objects on an inclined plane is a common scenario in which vectors need to be resolved
  - An inclined plane, or a slope, is a flat surface tilted at an angle,  $\theta$
- Instead of thinking of the component of the forces as horizontal and vertical, it is easier to think of them as **parallel** or **perpendicular** to the slope
- The **weight** of the object is vertically downwards and the **normal** (or reaction) force,  $R$  is always vertically up from the object
- The weight  $W$  is a vector and can be split into the following components:
  - $W \cos(\theta)$  perpendicular to the slope
  - $W \sin(\theta)$  parallel to the slope
- If there is no friction, the force  $W \sin(\theta)$  causes the object to move down the slope
- The object is not moving perpendicular to the slope, therefore, the normal force  $R = W \cos(\theta)$



*The weight vector of an object on an inclined plane can be split into its components parallel and perpendicular to the slope*

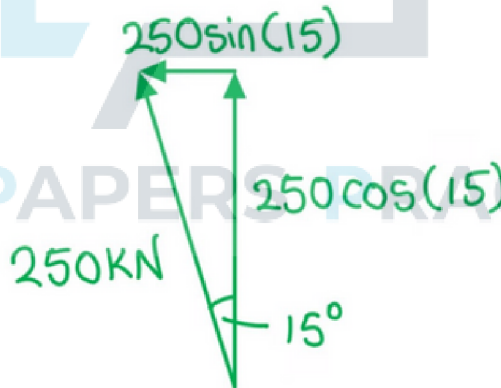
## ? Worked Example

A helicopter provides a lift of 250 kN when the blades are tilted at  $15^\circ$  from the vertical.



Calculate the horizontal and vertical components of the lift force.

**Step 1: Draw a vector triangle of the resolved forces**



**Step 2: Calculate the vertical component of the lift force**

$$\text{Vertical} = 250 \times \cos(15) = 242 \text{ kN}$$

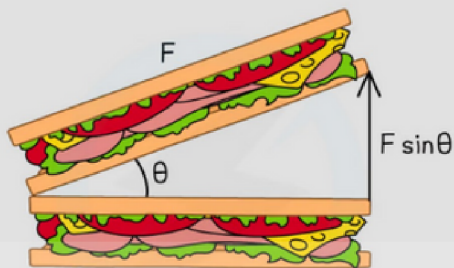
**Step 3: Calculate the horizontal component of the lift force**

$$\text{Horizontal} = 250 \times \sin(15) = 64.7 \text{ kN}$$



### Exam Tip

If you're unsure as to which component of the force is  $\cos \theta$  or  $\sin \theta$ , just remember that the  $\cos \theta$  is always the adjacent side of the right-angled triangle AKA, making a 'cos sandwich'



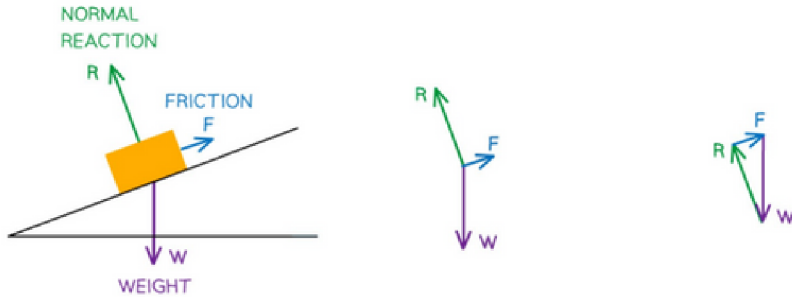
$F \cos \theta$

"cos SANDWICH"

### Equilibrium

- Coplanar forces can be represented by vector triangles
- Forces are in equilibrium if an object is either
  - At rest
  - Moving at **constant** velocity
- In equilibrium, coplanar forces are represented by **closed** vector triangles
  - The vectors, when joined together, form a closed path
- The most common forces on objects are
  - Weight
  - Normal reaction force
  - Tension (from cords and strings)
  - Friction
- The forces on a body in equilibrium are demonstrated below:

A VEHICLE IS AT REST ON A SLOPE AND HAS THREE FORCES ACTING ON IT TO KEEP IT IN EQUILIBRIUM



**STEP 1:**  
DRAW ALL THE FORCES ON THE FREE-BODY DIAGRAM

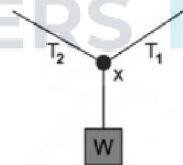
**STEP 2:**  
REMOVE THE OBJECT AND PUT ALL THE FORCES COMING FROM A SINGLE POINT

**STEP 3:**  
REARRANGE THE FORCES INTO A CLOSED VECTOR TRIANGLE. KEEP THE SAME LENGTH AND DIRECTION

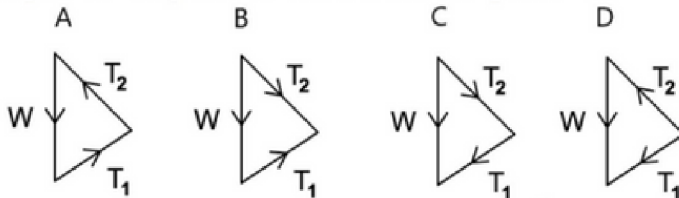
*Three forces on an object in equilibrium form a closed vector triangle*

? **Worked Example**

A weight hangs in equilibrium from a cable at point X. The tensions in the cables are  $T_1$  and  $T_2$  as shown.



Which diagram correctly represents the forces acting at point X?



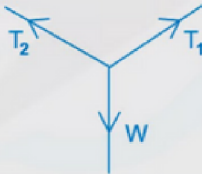




ANSWER: A

STEP 1

IDENTIFY THE DIRECTION OF ALL THE FORCES



STEP 2

ARRANGE THESE INTO A VECTOR TRIANGLE KEEPING THE SAME MAGNITUDE AND DIRECTIONS



STEP 3

ENSURE THE DIRECTION OF THE VECTORS FORM A CLOSED PATH



### Exam Tip

The diagrams in exam questions about this topic could ask you to draw to scale, so make sure you have a ruler handy!