3.6 Optimisation algorithms Vectors Mark Scheme

Q1.

(a) **All marks AO2 (analyse)**

	1	**2**	**3**	**4**	**5**	**6**
1	0	2	5	3	0	8
2	2	0	1	0	0	0
3	5	1	0	0	0	4
4	3	0	0	0	1	0
5	0	0	0	1	0	5
6	8	0	4	0	5	0

Alternative answer

	1	**2**	**3**	**4**	**5**	**6**
1	0	2	5	3	0	8
2		0	1	0	0	0
3			0	0	0	4
4				0	1	0
5					0	5
6						0

Alternative answer

	1	**2**	**3**	**4**	**5**	**6**
1	0					
2	2	0				
3	5	1	0			
4	3	0	0	0		
5	0	0	0	1	0	
6	8	0	4	0	5	0

Mark as follows:

1 mark 0s in correct places

1 mark all other values correct

I. non-zero symbols used to denote no edge but only for showing no edge going from a node to itself

2

(b) **All marks for AO1 (understanding)**

Adjacency list appropriate when there are few edges between vertices // when graph/matrix is sparse; **NE.** few edges

Adjacency list appropriate when edges rarely changed;

Adjacency list appropriate when presence/absence of specific edges does not need to be tested (frequently);

A. Alternative words which describe edge, eg connection, line, arc

Max 2

2

(c) **Mark is for AO2 (apply)**

It contains a cycle / cycles;

1

(d) **Mark for AO1 (knowledge)**

A graph where each edge has a weight/value associated with it;

1

(e) **All marks AO2 (apply)**

Mark as follows:

I. output column
1 mark first value of `A` is 2
1 mark second value of `A` is 5 and third value is 3
1 mark fourth and subsequent values of `A` are 8, 3, 7, 4, 9 with no more values after this
1 mark `D[2]` is set to 2 and then does not change

				D						P					
U	Q	V	A	1	2	3	4	5	6	1	2	3	4	5	6
-	1,2,3,4,5,6	-	-	20	20	20	20	20	20	-1	-1	-1	-1	-1	-1
				0											
1	2,3,4,5,6	2	2		2						1				
		3	5			5						1			
		4	3				3						1		
		6	8						8						1
2	3,4,5,6	3	3			3						2			
3	4,5,6	6	7						7						3
4	5,6	5	4					4						4	
5	6	6	9												
6	-														

1 mark `D[3]` is set to 5 and then changes to 3 and does not change again
1 mark correct final values for each position of array `P`

				D						P					
U	Q	V	A	1	2	3	4	5	6	1	2	3	4	5	6
-	1,2,3,4,5,6	-	-	20	20	20	20	20	20	-1	-1	-1	-1	-1	-1
				0											
1	2,3,4,5,6	2	2		2						1				
		3	5			5						1			
		4	3				3						1		
		6	8						8						1
2	3,4,5,6	3	3			3						2			
3	4,5,6	6	7						7						3
4	5,6	5	4					4						4	
5	6	6	9												
6	-														

1 mark correct final values for `D[1]`, `D[4]`, `D[5]`, `D[6]`

				D						P					
U	Q	V	A	1	2	3	4	5	6	1	2	3	4	5	6
-	1,2,3,4,5,6	-	-	20	20	20	20	20	20	-1	-1	-1	-1	-1	-1
				0											
1	2,3,4,5,6	2	2		2						1				
		3	5			5						1			
		4	3				3						1		
		6	8						8						1
2	3,4,5,6	3	3			3						2			
3	4,5,6	6	7						7						3
4	5,6	5	4					4						4	
5	6	6	9												
6	-														

Max 6 marks if any errors

7

(f) **Mark is for AO2 (analyse)**

The shortest distance / time between locations/nodes 1 and 6;

NE distance / time between locations/nodes 1 and 6

R. shortest route / path

1

(g) **All marks AO2 (analyse)**

Used to store the previous node/location in the path (to this node);

Allows the path (from node/location 1 to any other node/location) to be recreated // stores the path (from node/location 1 to any other node/location);

Max 1 if not clear that the values represent the shortest path

Alternative answer

Used to store the nodes that should be traversed;

And the order that they should be traversed;

Max 1 if not clear that the values represent the shortest path

2

[16]

Q1.

In previous years there have been questions asking students to complete an adjacency matrix based on a diagram of a graph and most students were able to answer question (a) this year. This was the first time that an adjacency matrix for a weighted graph had been asked for and some students had clearly not seen this type of question before and only included an indicator that there was an edge between two nodes rather than the weight of the edge between the two nodes; this meant they only got one of the two marks available for this question.

Questions (b)-(d) were about graph theory. Question (c) was well-answered with students identifying that it was not a tree because there were cycles. The most common incorrect answer was to say that it wasn't a tree because the edges have weights associated with them. Question (d) was also well-answered. Answers to (b) often showed that students were not as familiar with adjacency lists as they are with adjacency matrices.

For question (e) students had to complete a trace of Djikstra's Algorithm. This topic was not on the previous A-level specification and was often poorly answered suggesting many students had not tried to complete a trace for the algorithm before. For question (f) many students gave an answer that explained the point of Djikstra's Algorithm (find the shortest route from a node to each other node) rather than what the specific output in the algorithm given in the question would be (the distance of the shortest route from node 1 to node 6).