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Centre number	Candidate number
Surname	
Forename(s)	
Candidate signature	

A-level FURTHER MATHEMATICS

Paper 3 - Statistics

Exam Date Morning Time allowed: 2 hours

Materials

For this paper you must have:

- You must ensure you have the other optional question paper/answer booklet for which you are entered (either Mechanics or Discrete). You will have 2 hours to complete both papers.
- The AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should be used for drawing.
- Answer all questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 50.

Advice

Unless stated otherwise, you may quote formulae, without proof, from the booklet. You do not necessarily need to use all the space provided.

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A χ^2 -test for association is carried out on frequency data given in a 5 \times 3 contingency table using the 5% level of significance. All expected frequencies are greater than 5 State the number of degrees of freedom for this test.

Circle your answer.

[1 mark]

6 8 14 15

2	The continuous random variable Y has cumulative	distribution functio	n defined by

$$F(y) = \begin{cases} 0 & y < 0 \\ \frac{y^2}{36} & 0 \le y \le 6 \\ 1 & y > 6 \end{cases}$$

Find the value of P(Y > 4)

Circle your answer.

[1 mark]

$$\frac{4}{9}$$

$$\frac{16}{27}$$

$$\frac{11}{27}$$

3 The continuous random variable R follows a rectangular distribution with probability density function given by

$$f(r) = \begin{cases} k & -a \le r \le b \\ 0 & \text{otherwise} \end{cases}$$

Prove, using integration, th	$nat E(R) = \frac{1}{2}$	(b-a)
Prove, using integration, th	nat E(<i>R</i>) = — 2	(b-a)

[4 marks]

4		hs, in	centime	etres, o							e measures of lizard. His	
		53.2	57.8	55.3	58.9	59.0	60.2	61.8	62.3	65.4	66.5	
	The leng	ths ma	ay be a	ssumed	d to be n	ormally	distribu	ıted.				
	David co	rrectly	constr	ucted a	90% co	nfidence	e interv	al for th	e mear	length	of lizard	
	using the	e meas	sured le	engths o	given an	d the for	mula \bar{x}	$\overline{z} \pm \left(b \times \frac{1}{2}\right)$	$\frac{s}{\sqrt{n}}$			
	This inte	rval ha	ad limits	s of 57.6	63 and 6	62.45, cc	orrect to	two de	cimal p	laces.		
4 (a)	State the	value	for b u	ised in I	David's f	formula.					[1 ma	ark]
4 (b)	David int	erpret	s his in	terval a	nd state	s,						
	"My conf this partic					•		•	•	n of liza	rd lengths f	or
	Do you tl	hink D	avid's s	stateme	nt is true	e? Expla	ain your	reason	ing.		[2 ma	rks]

4 (c)	David's assistant, Amina, correctly constructs a $\beta\%$ confidence interval from David's random sample of measured lengths.						
	Amina informs David that the width of her confidence interval is 8.54.						
	Find the value of $oldsymbol{eta}$.	arks]					

Turn over for the next question

5	Students at a science department of a university are offered the opportunity to study an optional language module, either German or Mandarin, during their second year of study.						
	From a sample of 50 students who opted to study a language module, 31 were female. Of those who opted to study Mandarin, 8 were female and 12 were male.						
	Test, using the 5% level of significance, whether choice of language is independent of						
	gender. The sample of students may be regarded as random. [8 marks]						

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Turn over for the next question

6	The random variable T can take the value $T = -2$ or any value in the range $0 \le T < 12$
	The distribution of T is given by $P(T=-2)=c$, $P(0 \le T \le t)=225k-k(15-t)^2$
6 (a) (i)	Show that $1-c=216k$ [3 marks]

(4) (11)) Given that $c = 0.1$, find the value of $E(T)$	[3 mar
(b)	Show that $E(\sqrt{ T }) = \frac{5\sqrt{2} + 52\sqrt{3}}{52}$	
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7	Petroxide Industries produces a chemical used in the production of mobile phone covers
	for a mobile phone company.

The chemical becomes less effective when the mean level of impurity is greater than 3 per cent.

Sunita is the Quality Control manager at Petroxide Industries. After a complaint from the mobile phone company, Sunita obtains a random sample of this chemical from 9 batches.

She measures the level of impurity, X per cent, in each sample.

The summarised results are as follows.

$$\sum x = 28.8 \qquad \qquad \sum (x - \overline{x})^2 = 0.6$$

7 (a) (i)	Investigate using the 5% level of significance whether the mean level of impurity chemical is greater than 3 per cent.	level of impurity in the	
		7 marks]	

7	(a) (ii)	State the assumption that it was necessary for you to make in order for the test in part (a)(i) to be valid.	
		[1 mark]	
7	(b)	State the changes that would be required to your test in part (a) if you were told that the standard deviation of the level of impurity is known to be 0.25 per cent. [2 marks]	

Turn over for the next question

8	The time in hours to failure of a component may be modelled by an expone distribution with parameter $\lambda = 0.025$	ential
	In a manufacturing process, the machine involved uses one of these comp continuously until it fails.	onents
	The component is then immediately replaced.	
8 (a)	Write down the mean time to failure for a component.	[1 mark]
8 (b)	Find the probability that a component will fail during a 12-hour shift.	[1 mark]
8 (c)	A component has not failed for 30 hours. Find the probability that this com for at least another 30 hours.	ponent lasts [2 marks]

8	(d)	Find the probability that a component does not fail during 4 consecutive 12-hour shifts. [3 marks]
		•
8	(e) (i)	State the distribution that can be used to model the number of components that fail during one hour of the manufacturing process.
		[2 marks]
8	(e) (ii)	Hence, or otherwise, find the probability that no components fail during 5 consecutive
		12-hour shifts. [2 marks]
		END OF QUESTIONS

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