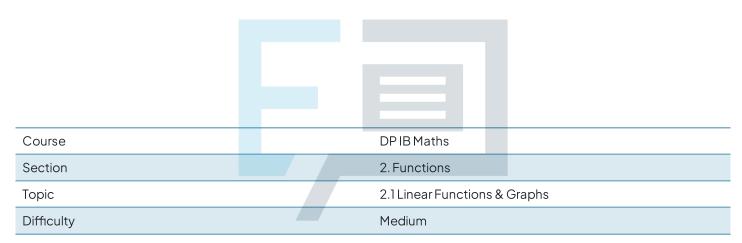


2.1 Linear Functions & Graphs

Mark Schemes



Exam Papers Practice

To be used by all students preparing for DP IB Maths AA SL Students of other boards may also find this useful



a) i) The y-intercept is when
$$x = 0$$
.
 $2(0) - y + 6 = 0$

ii) The x-intercept is when y=0.

- mi) Rearrange Li into the form y= moe + c,
- Examer Distribute Practice

$$y = 2x + 6 = 0$$
 + y and rearrange



$$M_2 = -\frac{1}{M_1}$$

$$M_{2} = -\frac{1}{2}$$

point (4,0) and
$$m_2 = -\frac{1}{2}$$

$$y-0=-\frac{1}{2}(x-4)$$

expand RHS

$$y = -\frac{1}{2}x + 2$$

× 2

rearrange to make

a, b and c integers



$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$

(in formula booklet)

Sub A and B into formula to find M.

$$M = \left(\frac{2+(-8)}{2}, \frac{8+2}{2}\right)$$

$$M = \left(\frac{-6}{2}, \frac{10}{2}\right)$$

$$M = (-3, 5)$$



$$M = \underline{y_2 - y_1}$$

Exam = $\frac{y_2 - y_1}{x_2 - x_3}$ (in formula booklet)

A(2,8)

B(-8,2)

Sub A and B into tormula to find m.

$$M_1 = \frac{2-8}{-8-2}$$

$$M_1 = \frac{-6}{-10}$$

$$M_1 = \frac{3}{5}$$



c) Point - gradient formula

$$y - y_1 = m(x - x_1)$$
 (in formula booklet)

*A(2,8) $m_1 = \frac{3}{5}$

Sub A and m, into $y - y_1 = m(x - x_1)$.

 $y - 8 = \frac{3}{5}(x - 2)$ expand RHS

 $y - 8 = \frac{3}{5}x - \frac{6}{5}$

Sy - 40 = 3x - 6

 $x + 34 = 0$ rearrange to make

 $x + 3x - 5y + 34 = 0$ and c integers

*NB. You could also use B.

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a) Midpoint formula

$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$

(in formula booklet)

Sub A and B into formula to find M.

$$M = \left(\frac{1+5}{2}, \frac{7+5}{2}\right)$$

$$M = \left(\frac{6}{2} \cdot \frac{12}{2}\right)$$

$$M = (3, 6)$$

b) Gradient formula

$$M = \underbrace{y_2 - y_1}_{\varkappa_2 - \varkappa_1}$$

(in formula booklet)

Example B (5,5)

Bub A and B into Formula to find

$$M_1 = \frac{5-7}{5-1}$$
 $M_2 = \frac{1}{2}$

Sub A and m, into y-y, = m(x-x,).

$$y-7=-\frac{1}{2}(2c-1)$$
 expand RHS
 $y-7=-\frac{1}{2}z+\frac{1}{2}$

$$y-7=-\frac{1}{2}x+\frac{1}{2}$$

$$y = -\frac{1}{2}x + \frac{15}{2}$$



c) le is perpendicular to li and passes through M.

Perpendicular gradients

$$M_2 = -\frac{1}{m_1}$$
 $M_1 = -\frac{1}{2}$

$$M_1 = -\frac{1}{2}$$

$$M_2 = 2$$

$$M(3,6)$$
 and $m_2=2$

Sub M and m2 into y-4. = m(x-x.).

a) Identify the finear function. acti

m = \$15/hour (hourly rate)



b) Sub
$$t=7$$
 into C_A .
 $C_A = 15(7) + 25$
 $C_A = 130



a) Gradient tormula

$$M = \frac{g_2 - g_1}{x_2 - x_1}$$
 (in formula booklet)

A(0,10) B(5,0)

Sub A and B into formula.

 $M_1 = \frac{0-10}{5-0}$ $\therefore m_1 = -2$

Sub A and m, into $y - y_1 = m(x - x_1)$.

 $y - 10 = -2(x - 0)$ expand RHS

 $y = -2x + 10$

EX b) Distance between two points formula CC

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$
 (in formula booklet)
$$A(0, 10) \quad B(5, 0)$$
Sub A and B into formula.
$$d = \sqrt{(0-5)^2 + (10-0)^2}$$

d= 11.2 units



$$y-0=-2(x-8)$$



a) Linear relationship:
$$y = mx + c$$

 $122 = m(115) + c$ $190 = m(200) + c$
solve simultaneous equations using your GOC.

$$M = 0.8$$
 and $c = 30$

: Photocopy shop B is cheaper.



a) Linear relationship: y= mx + c

b) Set both cost functions equal to each other.

Solve using your GDC.

$$x = 750$$

Monthly energy consumption = 750 kWh



a) Linear function:
$$C(x) = M9C + C$$
 $M = \frac{change}{change} \frac{in}{in} \frac{expenditure}{change} = \frac{change}{change} \frac{in}{in} \frac{C(x)}{change} \frac{in}{in} \times C(x)$
 $M = \frac{*AC(x)}{A \times x}$
 $A = \frac{*AC(x)}{A \times x}$
 $A = \frac{*Change}{A \times x} \frac{in}{in} \times C(x)$

Sub $AC(x)$ and $A = \frac{in}{in} \text{ formula}$.

 $M = \frac{60}{150}$
 $C(x) = 1000 \times 1200 \text{ m} = 0.4$ ($C(x) = 1000$)

Sub $C(x)$, x and x into formula.

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c) Sub
$$C(x) = 1070$$
 and solve for x .
 $0.4x + 520 = 1070$
 $0.4x = 550$
 $x = \frac{550}{0.4}$
 $x = 1375

Two points on Ware (0,0) and (20,8). Sub points into gradient formula.

$$M = 8.0$$
 $20-0$
 $M = 0.4$

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b) Find the equation of the east slope.

point (20,8) and
$$m = -\frac{3}{10}$$
 $y = 8 = -\frac{3}{10}(x - 20)$
 $y = -\frac{3}{10}x + 14$

Find the x-intersect of the east slope.

 $0 = -\frac{3}{10}x + 14$
 $\frac{3}{10}x = 14$
 $x = \frac{140}{3}$
 $x \cdot \text{intersect}$ at $(\frac{140}{3}, 0)$

Distance between two points formula

 $d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ (in formula

$$d = J(x_1 - x_2)^2 + (y_1 - y_2)^2$$
 (in formula bookle
Total distance = west slope + east slope.
West points are (0,0) and (20,8).
East points are (20,8) and ($\frac{140}{8}$,0).

d= /(0-20)2+(0-8)2+ /(20-140)2+ (8-0)2

d = 49.4 units

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c) Real life vs. mathematical model Any valid reason with an explanation is needed

The actual total distance may be greater than the answer in part (b) because the slope of a mountain is not constant.



Question 10 a) i) Sub (17.0) and (0,17) into gradient formula.

$$M_1 = \frac{17-0}{0-17}$$

Sub (17.0) and m_1 into $y - y_1 = m(x - x_1)$.

 $y - 0 = -1(x - 17)$

ii) Sub (2.0) and (0,-1) into gradient formula.

 $m_2 = \frac{-1-0}{0-2}$

Sub (2.0) and m_2 into $y - y_1 = m(x - x_1)$.

 $y - 0 = \frac{1}{2}(x - 2)$

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b) Shaded region forms a triangle.

Area of a triangle formula $A = \frac{1}{2}bh$ (in formula booklet)

b is the base, h is the perpendicular height b is formed by the x-intercepts of L_1 and L_2 , (17,0) and (2,0) respectively. b = 17 - 2 b = 15 units

h is the y-coordinate where L_1 and L_2 intersect Find where L_1 and L_2 intersect.

Intersection = (12,5) h = 5Sub b and h into formula. $A = \frac{1}{2}(15)(5)$

Exa An 37.5 units rs Practice



Question 11 a) PERPENDICULAR GRADIENT

$$M_1 \times M_2 = -1$$
 $L_1 = 2C + y = 16$
 $y = mx + c$
 $y = x + c$
 y

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