



# 2.1 Linear Functions & Graphs

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✤ 2.1.1 Equations of a Straight Line



## 2.1.1 Equations of a Straight Line

## Equations of a Straight Line

#### How do I find the gradient of a straight line?

- Find two points that the line passes through with coordinates  $(x_1, y_1)$  and  $(x_2, y_2)$
- The gradient between these two points is calculated by

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

- This is given in the formula booklet
- The gradient of a straight line measures its **slope** 
  - A line with gradient 1 will go up 1 unit for every unit it goes to the right
  - A line with gradient -2 will go down two units for every unit it goes to the right

#### What are the equations of a straight line?

- y = mx + c
  - This is the gradient-intercept form
  - It clearly shows the gradient *m* and the *y*-intercept (0, c)
- $y y_1 = m(x x_1)$ 
  - This is the **point-gradient form**
  - It clearly shows the gradient m and a point on the line (x1, y1)
- ax + by + d = 0
  - This is the **general form**

• You can quickly get the x-intercept 
$$\left(-\frac{d}{a}, 0\right)$$
 and y-intercept  $\left(0, -\frac{d}{b}\right)$ 

#### How do I find an equation of a straight line?

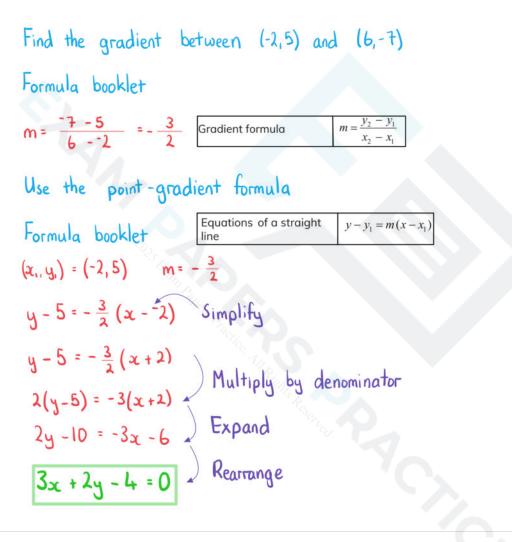
- You will need the gradient
  - If you are given two points then first find the gradient
- It is easiest to start with the point-gradient form
  - then rearrange into whatever form is required
    - multiplying both sides by any denominators will get rid of fractions
- You can check your answer by using your GDC
  - Graph your answer and check it goes through the point(s)
  - If you have two points then you can enter these in the statistics mode and find the regression line
    - y = ax + b



### Worked example

The line 1 passes through the points (-2, 5) and (6, -7).

Find the equation of 1, giving your answer in the form ax + by + d = 0 where a, b and d are integers to be found.

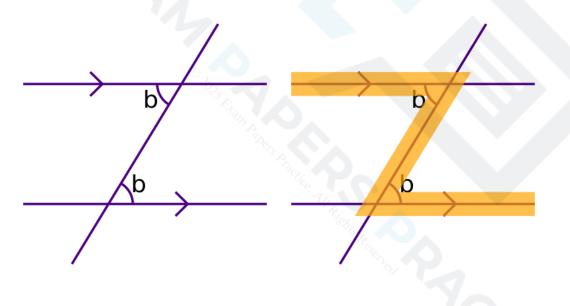




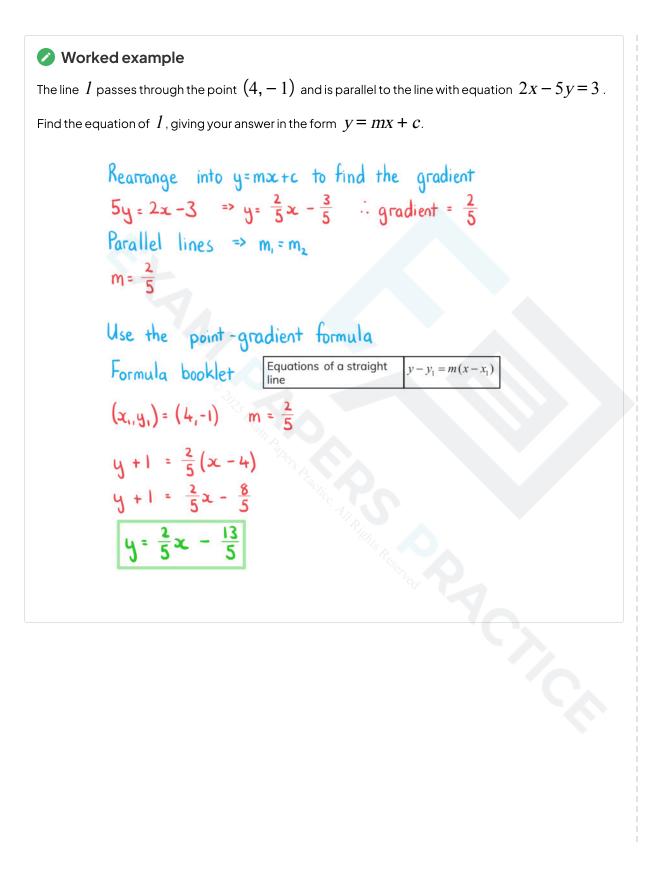
## Parallel Lines

#### How are the equations of parallel lines connected?

- Parallel lines are always equidistant meaning they never intersect
- Parallel lines have the same gradient
  - If the gradient of line  $l_1$  is  $m_1$  and gradient of line  $l_2$  is  $m_2$  then...
    - $m_1 = m_2 \Rightarrow l_1 \& l_2$  are parallel
    - $l_1 \& l_2$  are parallel  $\Rightarrow m_1 = m_2$
- To determine if two lines are parallel:
  - Rearrange into the gradient-intercept form y = mx + c
  - Compare the coefficients of X
  - If they are equal then the lines are parallel





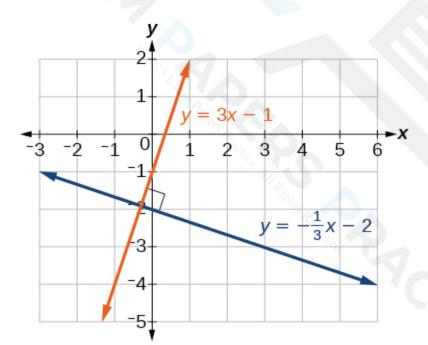




## **Perpendicular Lines**

#### How are the equations of perpendicular lines connected?

- **Perpendicular lines** intersect at right angles
- The gradients of two perpendicular lines are negative reciprocals
  - If the gradient of line  $l_1$  is  $m_1$  and gradient of line  $l_2$  is  $m_2$  then...
    - $m_1 \times m_2 = -1 \Rightarrow l_1 \& l_2$  are perpendicular
    - $l_1 \& l_2$  are perpendicular  $\Rightarrow m_1 \times m_2 = -1$
- To determine if two lines are perpendicular:
  - Rearrange into the gradient-intercept form y = mx + c
  - Compare the coefficients of X
  - If their product is -1 then they are perpendicular
- Be careful with horizontal and vertical lines
  - x = p and y = q are perpendicular where p and q are constants





#### Worked example

The line  $l_1$  is given by the equation 3x - 5y = 7.

The line  $I_2$  is given by the equation  $y = \frac{1}{4} - \frac{5}{3}x$ .

Determine whether  $I_1$  and  $I_2$  are perpendicular. Give a reason for your answer.

Rearrange L, into y = mx + c form  $5y = 3x - 7 \implies y = \frac{3}{5}x - \frac{7}{5}$ Identity gradients  $m_1 = \frac{3}{5} \qquad m_2 = -\frac{5}{3}$   $m_1 \times m_2 = -1 \implies$  Perpendicular lines  $\frac{3}{5} \times -\frac{5}{3} = -1$ L, and L<sub>2</sub> are perpendicular as  $m_1 \times m_2 = -1$