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1.4 Proof & Reasoning

IB Maths - Revision Notes

AA SL



1.4.1 Proof

Language of Proof

What is proof?

- Proof is a series of logical steps which show a result is **true** for all specified numbers
 - 'Seeing' that a result works for a few numbers is not enough to **show** that it will work for all numbers
 - Proof allows us to show (usually algebraically) that the result will work for **all values**
- You must be familiar with the notation and language of proof
- LHS and RHS are standard abbreviations for left-hand side and right-hand side
- Integers are used frequently in the language of proof
 - The set of **integers** is denoted by \mathbb{Z}
 - The set of **positive integers** is denoted by \mathbb{Z}^+

How do we prove a statement is true for all values?

- Most of the time you will need to use algebra to show that the left-hand side (LHS) is the same as the right-hand side (RHS)
 - You **must not** move terms from one side to the other
 - Start with one side (usually the LHS) and manipulate it to show that it is the same as the other
- A mathematical identity is a statement that is true for all values of x(or θ in trigonometry)
 - The symbol ≡ is used to identify an identity
 - If you see this symbol then you can use proof methods to show it is true
- You can complete your proof by stating that RHS = LHS or writing QED

💽 Exam Tip

© 2024 EXYou will need to show each step of your proof clearly and set out your method in a logical manner in the exam

Be careful not to skip steps







Proof by Deduction

What is proof by deduction?

• A mathematical and logical argument that shows that a result is true

How do we do proof by deduction?

- A proof by deduction question will often involve showing that a result is true for all integers, consecutive integers or even or odd numbers
 - You can begin by letting an integer be *n*
 - Use conventions for even (2n) and odd (2n 1) numbers
- You will need to be familiar with sets of numbers (ℕ, ℤ, ℚ, ℝ)
 - N the set of **natural numbers**
 - \mathbb{Z} the set of integers
 - Q the set of quotients (rational numbers)
 - \mathbb{R} the set of **real numbers**



😧 Exam Tip

- Try the result you are proving with a few different values
 - Use a sequence of them (eg 1, 2, 3)
 - Try different types of numbers (positive, negative, zero)
- This may help you see a pattern and spot what is going on





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